Optimal Control of the Vehicle Path Following by Using Image Processing Approach

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P A P E R  I N F O

A B S T R A C T

Nowadays, the importance of the vehicles and its dramatic effects on transportation system is obvious. The use of trailers with multiple axels for transporting bulky and heavy equipment is essential. Stability and steerability of trailers with multiple axels and wheels is one of the main concerns in the transportation system. Therefore, in this paper dynamic modeling and control of a 5 axal trailer was studied. As well as to increase maneuverability and speed up, 3 axles was considered to be steered. Also, by using image processing trailer path following in desired path with the highest accuracy was achieved. In this study, first a 14 DoF model for a 5 axal trailer with 3 steering axles was considered and its dynamic was formulated. For this purpose, dynamic equations including kinematic and kinetic of trailer was obtained. Then, with evaluating trailers response, a linear quadratic optimal control algorithm was designed. In order to evaluate the performance of the control algorithm, control problem simulation for single lane change and overtaking was done. The results confirmed the performance of designed control algorithm and image processing accuracy in trailer path following.


1. INTRODUCTION

In the last two decades, the use of articulated tracked vehicles has increased dramatically. The reason for this is the restrictions on driving single tracked vehicles. Today, articulated tracked vehicles are widely used in industries. Articulated tracked vehicles can be used as transporter, heavy equipment [1] or in agriculture field [2]. They can be used as desert transporters or carriers of passengers on the snow or sand terrains. They can also be used as forest fire tracked vehicles [3]. In addition to the reasons and as the most important reason, they can be used invaluable in the field of military vehicles for pulling tracked trailers and towing knocked out tanks from the battlefield [4]. Maneuverability articulated tracked vehicles can be excellent, because it usually needs less power to bypass than single tracked vehicles. Improving obstacle crossing and uniform ground pressure are the benefits of articulation to towing vehicles [5, 6]. A lot of ease is created by articulation, because it allows the path to match the ground, resulting in more integrated pressure. Slender vehicles are less likely to be at the same level of contact with obstacles and less resistance to short and wider vehicles. Although there is a straightening up problem when steering a car. This problem occurs in the wagon type of articulated tracked vehicles [7]. Alhimdani and his colleagues [8] try to solve this problem in theory the use of a hydraulic piston. Although it was found that this method is not practical and practical, the problem has not been completely solved yet. A new idea for the steering problem was suggested during the right maneuvering of a towed vehicle, and it was the use of high tension ropes (high strength) to tow a trailer chasing trailer by a towing vehicle [9]. Two loose ropes were used when they were bypassed, when straightening up one of the ropes was pulled. Luijten [10] in addition to the conventional combinations of tractor-semi-trailer, truck - central axle trailer, truck-full trailer, ecomobies; taller and heavier truck combinations; as a test and experience in the Netherlands. Safety is a common concern among all road users, challenged by the volume of traffic that has actually grown in recent years and is projected to rise further in the future. For this purpose, in literature [11] put their emphasis on commercial heavy-duty vehicles and considered tractors

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as semi-trailer as the basis for their studies. For this purpose, they have developed two dynamic models in the lateral control of a trailer - semi-trailer; a complex simulation model and two simplified control models. In their report, a complex nonlinear model has been developed to simulate the dynamic responses of tractor-to-trailer vehicles, which has been used to evaluate the efficiency of the lateral control algorithm. The articulated vehicle is most commonly composed of two main parts of the tractor unit and trailer unit. Due to the more complex dynamical structure and the height of the center of gravity, they have a more detailed car than a riding vehicle have less motor stability [12, 13]. Schmid [14] studied the dynamical stability of a tractor-trailer by analyzing linear equations. He has used the Routh Hurwitz Criteria to detect and instability. An analysis by Fakoor et al. [15] has shown that the nominal position of the center of gravity in path following is one of the most important parameters in the stability. In existing research, the stability analysis of heavy vehicles is usually carried out using the two main methods of Routh Hurwitz and the solution of the specific value of the characteristic equation. Fakoor et al. [16] have examined the stability profile of the robot using special values analysis. They have developed a set of algebraic equations for determining the stability ranges of a trailer-mounted system. In his research, the general rule governing both oscillatory and non-oscillatory stability is derived using the Routh Hurwitz benchmark. The graphical expression of this analysis is presented as a stable region bounded by stable oscillatory boundaries and non-oscillatory stability. But it should be noted that increasing the number of axles and, in the long run, the trailer wheels will consider certain considerations for increasing the speed of transport, increased maneuverability, increased safety and better control, which will reduce the high cost of the SUV tires. Therefore, dynamic modeling and control of a 5-axle trailer have been investigated. Also, to increase maneuverability and increase the speed and speed of the vehicle’s route, the 3-axis steering of the trailer (axis 1, 4 and 5) was considered. In this paper, we first consider a 14-degree freedom model for a 5-axle trailer with 3 steering axles, and its characteristics are described. Then, the trajectory dynamics equations are extracted from the kinematic and kinetic equations. In this paper, an optimal linear square optimization algorithm is designed to examine the type of trailer behavior. Eventually, using the image processing algorithm, the path of the vehicle is identified along the road and is designed using the controller and the input of the road route from the algorithm of image processing, routing, and trailer movement. To test the performance of the control algorithm, the control problem is simulated for three single line switching maneuvers, dual line switching, and overtaking. The results confirm the validity of the control algorithm.

2. RESEARCH METHOD

Modeling in fact means extracting mathematical equations of the behavior of a system and approximating the system’s behavior by those equations. For example, different vehicle behaviors such as side and side behavior, longitudinal function, travel comfort, etc. can be approximated using a number of state-space equations, whose state variables are the same degrees of system freedom or derivatives. Modeling of automobile dynamic equations can be divided into two general categories: a) simple linear modeling and b) complex nonlinear modeling. Usually, a simple linear model for designing a system for maintaining the rotational stability of a vehicle using a steering input is used first, so that the design and implementation of the control system can be done at a lower cost. Then, considering that the behavior of the vehicle is highly nonlinear and cannot be used, a simple linear model to achieve the behavior of the vehicle in all its operating conditions, is used in a more complex model with more degrees of freedom to simulate vehicle behavior.

2. 1. Trailer Kinematics  In this section, the velocity and velocity are calculated according to the defined coordinate devices. Using the kinematics of the system, in other words, the system's transition and rotational velocities, kinetic energy, acceleration, kinetics and equations of motion of the system will be computable.

The objective in modeling is to evaluate the axial motion of the 5-axis trailer movement, which is visible in Figure 1 in its lateral view, and the upper. As shown in Figure 2, axes 1, 4, and 5 have the ability to steer. According to Figure 1 and coordinate devices, we will have:

\[
\begin{bmatrix}
    i_2 \\
    i_3 \\
    i_4
\end{bmatrix} = \begin{bmatrix}
    \cos \theta_2 & -\sin \theta_2 \\
    \sin \theta_2 & \cos \theta_2
\end{bmatrix} \begin{bmatrix}
    i_0 \\
    u
\end{bmatrix}
\]

\[
\begin{bmatrix}
    i_2 \\
    i_3 \\
    i_4
\end{bmatrix} = \begin{bmatrix}
    1 & 0 & 0 \\
    0 & 1 & -\varphi \\
    0 & \varphi & 1
\end{bmatrix} \begin{bmatrix}
    i_0 \\
    s_0 \\
    s_2
\end{bmatrix}
\]

The trailer speed in each of the reference and unscreened coordinate systems will be in accordance with Equations (3) and (4), which is obtained by Equations (1) in (5) and (6).

\[
V_{CG} = \dot{x}_n i_n + \dot{y}_n j_n
\]

\[
V_{CG} = \dot{x}_u i_u + \dot{y}_u j_u
\]

\[
\dot{x}_n = \dot{x}_u \cos \theta_2 - \dot{y}_u \sin \theta_2
\]

\[
\dot{y}_n = \dot{x}_u \sin \theta_2 + \dot{y}_u \cos \theta_2
\]

The trailer acceleration in each of the coordinate devices according to Equations (7) and (8) will be achieved by placing Equation (1) in two Equations (9) and (10).
speed of the trailer is calculated as follows.

The trailer parameters shown in Figure 2 are presented in Table 1.

The angular velocity of the mass coordinate system with the ratio of the spring to the reference device is calculated according to Equation (11).

By deriving from each vector the coordinates of the system are:

The trailer parameters shown in Figure 2 are presented in Table 1.

Now, according to the calculations done and the relationship between the coordinate devices, the overall speed of the trailer is calculated as follows.

TABLE 1. Trailer parameters

<table>
<thead>
<tr>
<th>Definition</th>
<th>parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Height of the center of gravity trailer</td>
<td>$z_0$</td>
</tr>
<tr>
<td>Trailer axle spacing from the center of gravity trailer</td>
<td>$a_z$</td>
</tr>
<tr>
<td>Two trailer axle distance from the center of gravity trailer</td>
<td>$a_2$</td>
</tr>
<tr>
<td>Three-trailer axle distance from the center of gravity trailer</td>
<td>$a_3$</td>
</tr>
<tr>
<td>Four-trailer axle spacing from the center of gravity trailer</td>
<td>$a_4$</td>
</tr>
<tr>
<td>Five-trailer axle spacing from the center of gravity trailer</td>
<td>$a_5$</td>
</tr>
<tr>
<td>Half wheels in a trailer axle (half the width of the axle)</td>
<td>$b_2$</td>
</tr>
<tr>
<td>Radius trailer wheels</td>
<td>$r$</td>
</tr>
<tr>
<td>Trailer weight</td>
<td>$m_2$</td>
</tr>
<tr>
<td>The center of gravity trailer center of the system roll</td>
<td>$h_2$</td>
</tr>
</tbody>
</table>

2.2. Trailer Kinetics As shown in Figure 6, the model for a trailer is a 14 degree freedom model. Generalized system coordinates 10 axis of the wheel corresponding to 10 wheels, $x_n$ the position of the center of gravity of the trailer in the direction of the axis $x_n$, $y_n$ the position of the center of gravity of the trailer in the direction of the $y_n$ axis, the tractor roller angle $\theta$ and Yaw trailer angle $\phi$. The generalized coordinates that can be analyzed with the behavior of the system are as follows.

Lagrange method is used to obtain the equations of motion of the system. The general formula of Lagrange is as Equation (18).

\[
\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{q}_k} \right) - \frac{\partial L}{\partial q_k} + \frac{\partial \Phi}{\partial q_k} = f_k
\]
Where $q_k$ is the generalized k-th and Lagrange $L$ coordinate difference between the kinetic energy $T$ and the potential $f_k$ is the generalized k-th force.

$$L(q, \dot{q}) = T(q, \dot{q}) - U(q) = \frac{1}{2} \dot{q}^T B(q) \dot{q} - U(q)$$ (19)

$B(q)$ is a positive mechanical inertia matrix of the mechanical system.

$$F = \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \epsilon_{ij} q_i q_j$$ (20)

The kinetic energy of the system is equal to:

$$T = \frac{1}{2} m_2 v_{CGy/n} v_{CGz/n} + \frac{1}{2} I_{2z} \omega_{sy/n}^2$$ (21)

The potential energy of the system will be equal to:

$$U(q) = \frac{1}{2} k \phi^2 - m_2 g \phi_2 (1 - \cos \phi)$$ (22)

And $F$ is as follows:

$$F = \frac{1}{2} \ddot{\phi}^2$$ (23)

By calculating and simplifying, the equations of motion of the system in the system of low-intensity mass coordinates are calculated as follows:

$$m_2(\dot{x}_u + h_2 \phi \theta_2 - y_u \dot{\theta}_2 + 2 h_2 \dot{\phi} \theta_2) = F_{x_u}$$ (24)

$$m_2(\dot{y}_u - h_2 \phi \theta_2 + x_u \dot{\theta}_2 + 2 h_2 \phi \dot{\theta}_2) = F_{y_u}$$ (25)

$$m_2 h_2 \phi \theta_2 + (1 + (1 + m_2 h_2^2) \phi^2) \dot{\theta}_2 - m_2 h_2 \phi \ddot{\phi} \theta_2 = F_{\theta_2}$$ (27)

So, with this in mind, we are going to retrieve the generalized forces in the system of bumpy mass coordinates. The general force for $x_u$ is as follows:

$$F_{x_u} = f_{\dot{\theta}_1} \cos(\theta_2 - \theta_1) + f_{\dot{\theta}_1} \sin(\theta_2 - \theta_1) + (f_{\theta_1} + f_{\theta_2}) \cos \delta_1 + (f_{\theta_1} + f_{\theta_2}) \sin \delta_1 + (f_{\theta_2} + 2 f_{\theta_2}) \cos \delta_3 + (f_{\theta_1} + f_{\theta_2}) \sin \delta_3 + (f_{\delta_1} + f_{\delta_3}) \cos \delta_2 + (f_{\delta_1} + f_{\delta_3}) \sin \delta_5$$ (28)

The general force for $y_u$ is as follows:

$$F_{y_u} = -f_{\dot{\theta}_2} \sin(\theta_2 - \theta_1) + f_{\dot{\theta}_2} \cos(\theta_2 - \theta_1) + (f_{\theta_1} + f_{\theta_2}) \sin \delta_1 + (f_{\theta_1} + f_{\theta_2}) \cos \delta_1 + (f_{\theta_1} + f_{\theta_2}) \sin \delta_3 + (f_{\theta_1} + f_{\theta_2}) \cos \delta_3 + (f_{\theta_2} + 2 f_{\theta_2}) \cos \delta_5 + (f_{\theta_1} + f_{\theta_2}) \sin \delta_5$$ (29)

The general force for $\phi$ is as follows.

$$f_\phi = (f_{\theta_1} x_\phi \cos \phi) + f_{\theta_2} x_\phi \cos \phi + (f_{\theta_3} x_\phi \cos \phi) + (f_{\theta_4} x_\phi \cos \phi) + (f_{\theta_5} x_\phi \cos \phi) + (f_{\theta_3} x_\phi \cos \phi) + (f_{\theta_4} x_\phi \cos \phi) + (f_{\theta_5} x_\phi \cos \phi)$$ (30)

The general force for $\theta_2$ is as follows.

$$f_{\theta_2} = (f_{\delta_1} \cos(\theta_2 - \theta_1) - f_{\delta_2} \sin(\theta_1 - \theta_2) + (f_{\delta_1} + f_{\delta_2}) \cos \delta_1 + (f_{\delta_1} + f_{\delta_2}) \sin \delta_1 + (f_{\delta_1} + f_{\delta_2}) \sin \delta_3 + (f_{\delta_1} + f_{\delta_2}) \cos \delta_3 + (f_{\delta_2} + 2 f_{\delta_2}) \cos \delta_5 + (f_{\delta_1} + f_{\delta_2}) \sin \delta_5$$ (31)

### 3. DESIGNING A CONTROL ALGORITHM

The main purpose of this section is to design a control algorithm for lateral control of the system. For this purpose, a linearized model of the trailer dynamics is firstly extracted. Then, based on this linear model, an optimal linear square control algorithm is designed.

#### 3.1. Trailer Dynamics and its Linearization

To extract the dynamic model, the trailer is operated as follows:

$$m_2 (\ddot{x}_u + \dot{y}_u \dot{\theta}_2) = F_{x_u}$$ (32)

$$I_{12} \ddot{\theta}_2 = F_{\theta_2}$$ (33)

Given $\dot{x}_u = u$, $\dot{y}_u = v$ and $\dot{\theta}_2 = r$ we will have:

$$m_2 (v + ur) = F_{x_u}$$ (34)

$$I_{12} \dot{r} = F_{\theta_2}$$ (35)

To get the state of the system state, the system state variables are defined as follows.

$$x_1 = y_u$$

$$x_2 = y_u$$

$$x_3 = \dot{\theta}_1$$

$$x_4 = \dot{\theta}_1$$

$$x_5 = \dot{x}_u$$

With linearization, simplification, and computing we will:

$$\dot{x}_1 = x_2$$ (37)

$$\dot{x}_2 = -u x_4 + \frac{1}{m_2} \left( -\frac{2}{u} (c_1 + c_2 + c_3 + c_4) - c_3 x_2 - \frac{2}{u} (c_1 a_1 + c_2 a_2 - c_3 a_3 - c_4 a_4) - c_5 a_5 x_4 + 2 c_1 \delta_1 + 2 c_4 \delta_4 + 2 c_5 \delta_5 \right)$$ (38)

$$\dot{x}_3 = x_4$$ (39)

$$\dot{x}_4 = \frac{1}{I_{12}} \left( -\frac{2}{u} (c_1 a_1 + c_2 a_2 - c_3 a_3 - c_4 a_4) - c_5 a_5 x_4 + \frac{2}{u} (c_1 a_1^2 + c_2 a_2^2 - c_3 a_3^2 - c_4 a_4^2) - c_5 a_5^2 x_4 + 2 c_1 \delta_1 - 2 c_4 \delta_4 - 2 c_5 \delta_5 \right)$$ (40)

Regarding the linearization, we will have in state matrix:

$$\dot{x} = Ax + Bu, \quad y = Cx + Du$$ (41)
where in:

\[
A = \begin{bmatrix}
0 & 1 & 0 & 0 \\
0 & -1.0836 & 0 & -15.5834 \\
0 & 0 & 0 & 1 \\
0 & 0.1507 & 0 & -0.7534
\end{bmatrix}
\]  \hspace{1cm} (42)

\[
B = \begin{bmatrix}
0 & 0 & 0 & 3.6122 \\
0 & 0 & 0 & 3.6122 \\
1.5069 & -1.5069 & -2.5115
\end{bmatrix}
\]  \hspace{1cm} (43)

\[
C = \begin{bmatrix}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{bmatrix}, \quad D=0
\]  \hspace{1cm} (44)

3.2. Linear Quadratic Optimal Control

Linear square control optimal method is one of the most important optimal design methods in linear systems. The advantage of this method is the state vector feedback control method, which provides a systematic method for calculating the state vector feedback control matrix.

3.2.1. Linear Quadratic Regulator: Consider the Linear Time Invariant (LTI) system of \( \dot{x} = Ax + Bu \), the goal is to obtain the k-state vector feedback control \( u(t) = -kx \), in such a way that the following performance index is minimized.

\[
J = \int_{0}^{\infty} (x^TQx + u^TRu)dt
\]  \hspace{1cm} (45)

By inserting \( u(t) = -kx \) we will have:

\[
J = \int_{0}^{\infty} x^T(Q + k^TRk)xdt
\]  \hspace{1cm} (46)

For the above problem to be answered, the controller must first be stable. Therefore, at least unstable modes must be stable or, in a more comprehensive state of the system, must be controlled.

To better understand the control algorithm, the control diagram of Figure 4 can provide the correct image of the control system.

3.3. Image Processing

3.3.1. Image Processing Consists Essentially of the Following Three Steps

- Capture images with optical scanners or with cameras and digital sensors
- Image analysis and manipulation, including: data compression, image restoration and extraction of specific information from the image by the image processing process
- The last step in which the output result can be an image or a report of the information that was obtained at the stage of the analysis of the image in the previous step.

The purpose of the image processing in this paper is to provide an independent input system for the vehicle's routing control system, which includes image intensification and recovery, image retrieval, pattern measurement, image recognition, and the transmission of roadway information to the controller input (Figure 5).

For vehicle routing, using sensors mounted on a vehicle, the road profile is marked on the road and obstacle lines on the specified route, and the vehicle can accurately navigate the vehicle's path by adjusting the steering wheel and torque. Two pieces of information are extracted from the image: offset the path from the center of the image and the path gradient. Figure 6 shows the extraction feature in more detail. The image processing system output is used as an input for the controller. The solution used here is to use a proper command control, which is guided by a combination of outputs of the image processing step. The only changes required when changing the chassis type to the engine control functions and mapping between the output of the image processing step and the vehicle commands. Obviously, if the vehicle is on the left side of the image, it should turn to the left, so if the vehicle is on the right, it should go back to the right, and also have to rotate the path in the image. Figure 7 shows the process of image processing of the road with lines on it.

4. RESULTS

4.1. Uncontrolled system behavior

In this section, the behavior of the system is examined without controller, for this purpose the system response is calculated to the initial conditions without controller presence. The results are shown in Figures 8 to 10. What is clear from the results is that the response was unstable, indicating the need for a controller to be present.
4. 2. System Control Response to the Initial Conditions  The response to its initial conditions is also presented in Figures 9 and 10. The results obtained in comparison with the results of the previous section indicate the optimal performance of the designed control algorithm.

4. 3. Simulation for Standard Maneuvers  Considering the maneuver of replacing the single line for the trailer and performing the simulation of the results, the following is presented in Figures 11 to 20. What is clear from the results is the effectiveness of the control algorithm in controlling the trailer on this maneuver.

As shown in figure 16, the vehicle deviation from desired path remains below 0.1m over the lane change path while the heading error over the maneuver is less than 0.2 rad.

Figure 7. The variable \( y \) trailer position response in the vertical direction without a controller.

Figure 8. The variable \( \theta \) (yaw) response of the trailer in the vertical direction without the controller.

Figure 9. Variable response \( y \) of the trailer position in the vertical direction relative to the initial condition.

Figure 10. Variable response \( y' \) of the trailer on the horizons page relative to the initial conditions.

It shows the accuracy of proposed controller and image processing system in trailer path following.

Figure 11. Single trailer line shift maneuver on Vehicle.
Figure 12. Fourth axis of the trailer command in the single line switching maneuver (control input)

Figure 13. Trailer side position diagram in time in the single line switching maneuver

Figure 14. Yaw Trailer Angle Scale Based on Time in the single line switching maneuver

Figure 15. Timing of the Yaw (angular velocity) of the trailer in time in the single line switching maneuver

Figure 16. Trailer roll rate graph in time in the single line switching maneuver

Figure 17. The slip angle of the first axle trailer in terms of time in the single line switching maneuver

Figure 18. The slip angle of the second axle trailer in terms of time in the single line switching maneuver

Figure 19. The slip angle of the third axle trailer in terms of time in the single line switching maneuver
5. CONCLUSION

Regarding the fact that in recent years, less work has been done on modeling and controlling trailers themselves, especially trailers with multiple axles, in this research dynamic modeling and 5-axle trailer control were placed on the agenda. The first idea for increasing the trailer maneuver, improving its behavior, increasing the speed of the trailer in maneuvers, reducing the tire's tire speed and improving the system's control function to prevent the occurrence of Jack-Knifing phenomenon and other phenomena that cause trouble in controlling the trailer, driving ability axes are used. For this purpose, axle 1, 4 and 5 trailer are intended to be steering axles. In this paper, after introducing the 5 axles trailer system, a dynamic trailer modeling, which includes kinematics and trailer kinetics, was carried out and motor equations were extracted. Then, an optimal linear square control algorithm was introduced and based on this control algorithm, a controller for the trailer was designed. In order to ensure the operation of the control algorithm, several maneuvers were simulated. In the end, the simulation results were discussed on the results.

6. REFERENCES


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چکیده

امروزه اهمیت خودرو و تاثیرات چشمگیر آن بر سیستم حمل و نقل آشکار است. استفاده از تریلرها با چندین محور، برای حمل و نقل محصولات سنگین ضروری است. پیاده‌ریزی و فرم‌پذیری تریلر جدید محورهای یکی از مسائل اصلی در سیستم حمل و نقل است. نابرابری در این مقادیر، مدلسازی و کنترل دینامیکی تریلر دو محوره بررسی قرار گرفت. به علاوه برای بهبود ماشین‌بندی و سرعت بخشیدن، ۳ محور به عناوین فرم‌پذیری در نظر گرفته شدند. همچنین با استفاده از پردازش تصویر، سعی می‌شود تا مسیر تریلر در مسیر بگذراند با بالاترین دقت. پایداری و باعث شدن این دقت محور، ابتدا دانشجویان دانشگاه علوم پزشکی اراذی برای تریلر ۳ محوری ۵ محوری در مدل فرم‌پذیری مورد بررسی قرار گرفت و مدل دینامیکی آن آراپ شد. این مدل م燃料ات دینامیکی از جمله سینماتیک و سینتیک تریلر بدست آمده است. سپس با ارزیابی یک سیستم کنترل بهبود مطلوب خطای طراحی شد. به منظور ارزیابی عملکرد کنترل، شبیه‌سازی سیستم کنترل در طی مقرر قرار می‌گرفت و سپس کنترل کنترل در اجلاس شد. نتایج نشان داد که کنترل کنترل و سیستم پردازش تصویر طراحی شده دقت و کارایی عملکرد را دارد.