Application of Wavelet Neural Network in Forward Kinematics Solution of 6-RSU Co-axial Parallel Mechanism Based on Final Prediction Error

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Abstract

Application of artificial neural network (ANN) in forward kinematic solution (FKS) of a novel co-axial parallel mechanism with six degrees of freedom (6-DOF) is addressed in current work. The mechanism is known as six revolute-spherical-universal (RSU) and constructed by 6-RSU co-axial kinematic chains in parallel form. First, applying geometrical analysis and vectorial principles the kinematic model is extracted and inverse kinematics solution is done. Due to highly nonlinear characteristic of the model, forward kinematic solution for 6-RSU is so complicated. Therefore, ANN based on wavelet analysis, as a powerful solution, is designed and applied to solve FK problem. The minimum prediction risk principle with using final prediction error (FPE) is applied to find the best and optimum topology of our proposed neural network (WNN) in this paper. Furthermore, proposed wavelet WNN is developed to approximate the specific reference trajectories for manipulated platform of mechanism and the results are obtained. Comparing the extracted results by WNN with closed form solution (CFS) demonstrates the accuracy and efficiency of the proposed WNN.


1. Introduction

In recent decades, utilization of parallel mechanisms versus the serial manipulators are expanded due to their advantages as low inertia, high stiffness, high force-weight ratio and high acceleration [1-3]. Nevertheless, small size of work space in parallel mechanisms is major concern and lots of efforts have been made to improve it. One solution is to employ co-axial actuated arms that can rotate around a central base column like 6-RSU mechanism reported in literature [4]. Since kinematics solution of mechanisms are extensively necessary to design of mechanism, workspace analysis and provide control strategies, inverse and forward kinematic analysis of 6-RSU is considered in current contribution. Solution of inverse kinematic problem (IKP) in parallel mechanisms is straightforward and there are many solution methods such as geometric solution, efficient inverse kinematics method, analytic method, iterative method and screw theory. However, it is obvious that the forward kinematic solution for this kind of mechanisms are difficult and complicated. Consequently, numerical methods such as Newton-Raphson, were presented as an extensive and prevalent solution in spite of their explicit drawbacks including initial guess, convergence, local minimum problem and etc. In the literature, many different types of parallel mechanism were introduced and analyzed and kinematic solution is extensively investigated [5-8]. Huang et al. [9] proposed a novel 3DOF parallel mechanism included 3-(PRPR+PRS) kinematic chains as a machine tool. They have considered inverse and forward kinematic analysis and developed the stiffness model and dexterity of mechanism. Gao et al. [10] analyzed forward kinematic problem (FKP) of the joint variable space of the general Stewart platform mechanism applying pseudo-arc length homotopy continuation algorithm. They compared the results with those obtained by Newton–Raphson algorithm. Sadjadi et. al. [11] presented the solution of forward kinematics problem for a novel redundant parallel manipulator.
They provided a quasi-closed form solution by combination of the numerical and analytical method. Also, they employed MLP, RBF, PNN and ANFIS types of neural networks for their approach. Rahmani et al. [12] designed and analyzed a novel redundant hybrid manipulator included two similar Stewart mechanisms in serial form. They applied neural network training to solve forward kinematics. They used various types of neural networks (NN) such as multi-layer perceptron (MLP) and radial bias function (RBF) with various learning algorithms to approximate specific trajectories. Yi Lu et al. [13] illustrated a novel 5-DOF modular parallel mechanism for medical applications and studied kinematics, workspace and singularity analysis. Qazani et al. [14] have executed extensive investigations about HEXAROT parallel manipulator with a rotation-symmetric arm system. They have done Kinematic analysis and workspace determination. Moreover, they studied motion error of mechanism and presented mathematical model along with experimental validation [15].

In this paper, mathematical model of kinematic analysis for co-axial symmetric 6-RUS parallel mechanism is extracted using geometrical analysis and vectorial principles. Due to nonlinear relations between work-space and joint-space variables, forward kinematic solution for 6-RSU is too intricate. Hence, using learning algorithms and soft computing based on neural network a WNN is designed and employed to forward kinematic solution of 6-RSU. For this purpose, inverse kinematic analysis is applied to provide data for network training and verification. Furthermore, in current paper, I utilized the minimum prediction risk principle using final prediction error (FPE) to define the best and optimum topology of our proposed WNN. Current contribution, decreases and, in some cases, eliminates the serious drawbacks of traditional numerical methods such as initial guess, convergence, local minimum problem and computing time. Also, we implement wavelet neural network to track a specific trajectory in oscillating circle and semi-cardioidal spiral paths of manipulated platform. Finally, the comparison of the results obtained by WNN with the CFS indicates the accurate performance and efficiency of the proposed neural network algorithm.

2. DESCRIPTION OF 6-RSU MECHANISM

6-RSU parallel mechanism consists of a moving platform as end-effector connected to a base column via six identical kinematic chains (Figure 1). Each kinematic chain includes an upper arm attached from one end to the base column via revolute joint and to moving platform at its connection point via a 5-DOF interface link. Also, the link is connected to the moving platform via universal \( (U_i) \) and to the upper arm by spherical joints \( (S_i) \). Therefore, due to the configuration of kinematic chains, the mechanism is known as 6-RSU. Six revolute joints \( (R_i) \) on the base column are actuated joints and provide the whole motion of mechanism by rotational displacement around the base. To describe the motion of mechanism and for kinematic analysis, two frames were employed. First, base frame \( (^{m}O) \) is fixed and placed on the base column. Second, platform frame \( (^{m}O) \) attached to center of moving platform and moves along with the platform. The position and orientation of the moving platform can be observed relative to both \( (^{m}O) \) and \( (^{m}O) \).

The position of six connection points on the moving platform are illustrated with vector \( ^{m}p_i \) \((i=1,...,6)\) relative to \( (^{m}O) \) as:

\[
^{m}p_i = (P_{x_i}, P_{y_i}, P_{z_i}, 0, 1) \\
P_{x_i} = P_{x_j} - R \sin(\phi), P_{y_i} = P_{y_j} - R \cos(\pi/6 - \phi) \\
P_{z_i} = P_{z_j} - R \sin(\phi/3 - \phi), P_{x_i} = P_{x_j} + R \cos(\phi) \\
P_{z_i} = P_{z_j} + R \sin(\phi/6 - \phi), P_{x_i} = P_{x_j} + R \cos(\phi/3 - \phi)
\]

where, \( R \) is the radius of peripheral circle surrounds the manipulated platform and \( \phi \) is the angle shown in Figure 1. The geometrical specifications of the considered 6-RSU mechanism are summarized in Table 1.

The length vector of the \( i^{th} \) upper arm and interface link are denoted \( A_i \) and \( B_i \), respectively. Due to advantages of 6-RSU mechanism such as large work-space it is useful for working, repairing, positioning and assembling inside cylindrical spaces such as pipes and aircrafts.

![Image](image_url)  
**Figure 1.** Schematic of the 6-RSU Mechanism and Geometrical Description of the Manipulated Platform

<table>
<thead>
<tr>
<th>TABLE 1. Geometrical specifications of 6-RSU</th>
<th>a</th>
<th>b</th>
<th>h1</th>
<th>h2</th>
<th>h3</th>
<th>h4</th>
<th>h5</th>
<th>h6</th>
<th>h7</th>
<th>h8</th>
<th>R</th>
<th>( \phi )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.95</td>
<td>1.05</td>
<td>0.75</td>
<td>0.85</td>
<td>1.25</td>
<td>1.35</td>
<td>1.75</td>
<td>1.85</td>
<td>0.20</td>
<td>65.0</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(all dimensions are in m or deg)
3. KINEMATICS OF 6-RSU MECHANISM

Kinematics of mechanisms deals with the investigation of the mechanisms motion regarding to the geometrical constraints of their links and divided into IKP and FKP. In fact, IKP is to conclude the movements of mechanism in the joint-space from the movements of mechanisms in the work-space. In the other words and concerning of the 6-RSU mechanism, IKP involves mapping a known position \((x, y, z)\) and orientation \((\alpha, \beta, \gamma)\) of the moving manipulated platform center into the rotation angles of the actuated revolute joints \(\theta_i\) \((i = 1,...,6)\) for each arm. Whereas, FKP is vice versa and more complex than IKP.

According to the vectorial presentation of the mechanism, the length vector of the \(i^{th}\) upper arm is defined relative to base frame as:

\[
b_{A_i} = [A_i \cos \theta_i \quad A_i \sin \theta_i \quad h_i]^{T}
\]  

(2)

In which \(\theta_i\) is the angle between \(bXi\) of the base frame and the \(i^{th}\) upper arm and declares the rotation of the \(i^{th}\) upper arm around the base column. The position vector of each universal joint in base frame \(b_{P_i} = (b_{P_{ix}}, b_{P_{iy}}, b_{P_{iz}})^T\) is represented by homogeneous transformation matrix as follows:

\[
b_{P_i} = H_{bO}b_{A_i} = m_{P_i}
\]  

(3)

In which \(H_{bO}b_{A_i}\) is the homogeneous transformation matrices from frame \((bO)\) to frame \((bA_i)\) and are described as follows:

\[
H_{bO}b_{A_i} = \begin{bmatrix} R_{i1} & R_{i2} & R_{i3} & x \\ R_{i4} & R_{i5} & R_{i6} & y \\ R_{i7} & R_{i8} & R_{i9} & z \\ 0 & 0 & 0 & 1 \end{bmatrix}
\]  

(4)

where, position of \((bO)\) with respect to \((bA_i)\) is defined by \((x, y, z)\) and orientation of \((bO)\) is implied by Euler ZYZ convention as \([R_i] = R_{zyx} = R_{z}(\alpha)R_{y}(\beta)R_{y}(\gamma)\):

\[
\begin{bmatrix} Ca & Cb & Cy - Sa & Sy & -Cb & Cy & Sa & Cb & 0 \\ Sa & Cb & Cy & Ca & Cy & Sa & Cb & 0 & 0 \\ -Sy & Cy & Ca & Cy & Sa & Cb & 0 & 0 & 0 \end{bmatrix}
\]  

(5)

In which, \(C(.) = \cos(.)\), \(S(.) = \sin(.)\).

The length vector of the \(j^{th}\) interface link, \(b_{B_j}\), relative to the base frame \((bO)\) is expressed as:

\[
b_{B_j} = b_{P_j} - b_{A_j}
\]  

(6)

And the length is:

\[
b_{A_j} = [b_{A_j}]^2 = [b_{P_j} - b_{A_j}]^2
\]  

Substituting Equations (2), (3) into Equation (7) with some algebraic calculations resulted in:

\[
k_{13} + k_{13} \sin \theta_i + k_{13} \cos \theta_i = 0
\]  

(8)

where,

\[
k_{13} = 2x \cdot Ca \cdot Cb \cdot Cy \cdot (b_{P_{iy}} + b_{P_{iy}}) + 2y \cdot b_{P_{iy}} \cdot Sa \cdot Cb \cdot Cy
\]

+ \[
2(z - h_i) \cdot b_{P_{iy}} \cdot Sin \cdot Cy + 2x(z - h_i) \cdot b_{P_{iy}} \cdot Sin \cdot Cb \cdot Cy
\]

+ \[
2x(b_{P_{iy}} \cdot Cy - b_{P_{iy}} \cdot Sa \cdot Cb \cdot Cy - b_{P_{iy}} \cdot Sa \cdot Cb \cdot Cy)
\]

(9)

\[
k_{13} = -2A_i(xz - b_{P_{iy}} \cdot Sa \cdot Cy + b_{P_{iy}} \cdot Sa \cdot Cb \cdot Cy)
\]

+ \[
2y(b_{P_{iy}} \cdot Cb \cdot Cy + b_{P_{iy}} \cdot Sa \cdot Cb \cdot Cy)
\]

(10)

\[
k_{13} = -2A_i(xz - b_{P_{iy}} \cdot Sa \cdot Cy + b_{P_{iy}} \cdot Sa \cdot Cb \cdot Cy)
\]

+ \[
2y(b_{P_{iy}} \cdot Cb \cdot Cy + b_{P_{iy}} \cdot Sa \cdot Cb \cdot Cy)
\]

(11)

Substituting Equations (9)-(11) into Equation (8) yields to solution of \(\theta_i\) as:

\[
\theta_i = -2\arctan[k_{13} - \sqrt{(k_{13}^2 + k_{13}^2 + k_{13}^2)}/(k_{13} - k_{13})]
\]

(12)

for \(i = 1, 2, 5, 6\)

\[
\theta_i = -2\arctan[k_{13} + \sqrt{(k_{13}^2 + k_{13}^2 + k_{13}^2)}/(k_{13} - k_{13})]
\]

(12)

for \(i = 3, 4\)

Equation (12) is the solution for IKP of 6-RSU mechanism. As it is clear, the inverse kinematic analysis of 6-RSU mechanism is easy and straight forward. In FKP the position \((x, y, z)\) and the orientation \((\alpha, \beta, \gamma)\) of the moving manipulated platform center are unknown and should be determined based on known joint-space parameters. But, due to highly nonlinearity of kinematics model expressed in Equations (8) and (12), the mapping from known joint-space rotational angles \(\theta_i\) \((i = 1,...,6)\) into the pose of the moving platforms is so complicated. Therefore, wavelet based neural network is proposed and applied to solve the FKP of the 6-RSU mechanism in current work.

4. WAVELET NEURAL NETWORK

4. 1. Topology of WNN
The wavelet neural network (WNN) is an artificial neural network technique based on wavelet transformation [16, 17].
Convenient localization property in time domain, efficient ability to approximate complicated mappings and impressive learning ability are the main characteristics of WNN make it appropriate and successful in approximation of nonlinear systems. Furthermore, to avoid the local minimum problem in training procedure of the NN the WNN is superseded to neural networks which follow the availability of the rates of the convergence for approximation by wavelet based networks. Proposed WNN is constructed by association of neurons in forward pathway. In current contribution, a feed forward MIMO-WNN is designed with three input-hidden-output layers using wavelets as the activate functions of the hidden layer. The proposed WNN consist of m, p and n nodes in the input, hidden and output layers, respectively. The number p is defined by the minimum prediction risk principle with using final prediction error (FPE). Figure 2 illustrates the topology of the proposed WNN with the activate function of the $j^{th}$ node in the hidden layer as:

$$ \psi_{a_j b_j}(t) = \frac{1}{\sqrt{a_j}} \psi\left(\frac{t-b_j}{a_j}\right) \quad j = 1,2, ..., p $$

where, $\psi(t)$ is the wavelet function and chosen Morlet wavelet function and $f(t)$ is considered sigmoid function.

### 4.2. Training Algorithm

For training a feed forward networks the back propagation (BP) algorithm is the most useful and applicable [18, 19] and it is employed to train the proposed WNN. BP includes forward and backward passes. The output performance of the network is provided by the forward pass and the backward pass specifies the initial errors for each node of the network. So, for minimizing all specified errors the weights of the network are regulated. Since the input vector $X = (x_1, x_2, ..., x_n)$ is feed to the proposed WNN in Figure 2; the output of the $j^{th}$ node in hidden layer is defined as:

$$ \psi_{a_j b_j} \left( \sum_{k=1}^{m} w_{jk} x_k - \theta_{jk} \right) = \psi_{a_j b_j} \left( F_j^{(1)} - \theta_{jk} \right) $$

$$ F_j^{(1)} = \sum_{k=1}^{m} w_{jk} x_k - \theta_{jk} $$

The $i^{th}$ node of output layer yields to:

$$ y_i = f \left( \sum_{j=1}^{p} w_{ij} \psi_{a_j b_j} \left( F_j^{(1)} - \theta_{jk} \right) \right) = f(F_i^{(2)}) $$

$$ F_i^{(2)} = \sum_{j=1}^{p} w_{ij} \psi_{a_j b_j} \left( F_j^{(1)} - \theta_{jk} \right) $$

$Y = (y_1, y_2, ..., y_n)$ is determined as the output vector of the WNN by Equation (16). Therefore, the total error for the network should be minimized as considered as follows:

$$ E = \frac{1}{2} \sum_{q=1}^{Q} \sum_{i=1}^{n} (\bar{y}_q - y_q)^2 $$

(18)

In which, $Q$ is training samples, $\bar{y}_q = (\bar{y}_{q1}, \bar{y}_{q2}, ..., \bar{y}_{qn})$ and $Y_q = (y_{q1}, y_{q2}, ..., y_{qn})$ are the desired and trained WNN output vectors, respectively. For minimizing $E$, the iterative gradient descent method is employed to formulate the WNN parameters as follows:

$$ w_{ij}^{(2)}(t+1) = (1+\sigma)w_{ij}^{(2)}(t) - \sigma w_{ij}^{(2)}(t-1) - \lambda \frac{\partial E}{\partial w_{ij}^{(2)}} $$

$$ \theta_{ij}^{(2)}(t+1) = (1+\sigma)\theta_{ij}^{(2)}(t) - \sigma \theta_{ij}^{(2)}(t-1) - \lambda \frac{\partial E}{\partial \theta_{ij}^{(2)}} $$

$$ a_j(t+1) = (1+\sigma) a_j(t) - \sigma a_j(t-1) - \lambda \frac{\partial E}{\partial a_j} $$

$$ b_j(t+1) = (1+\sigma) b_j(t) - \sigma b_j(t-1) - \lambda \frac{\partial E}{\partial b_j} $$

In which, $t$ and $\lambda$ the are learning iteration index and the rate of learning, respectively. Also, $\sigma$ is the momentum factor and considered $0 < \sigma < 1$ to improve the rate of learning. The partial derivatives of the error $E$ respect to each parameter can be calculated easily.

### 4.3. Optimum Topology for WNN

Identification the optimum topology and correct construction of the network is most important steps in NN simulation which is included the number of hidden layers and the number of neurons in the hidden layers.

**Figure 2. Topology of the Proposed WNN**
Networks with more or fewer hidden units than needed, result in over-fitted model or poor learning the underlying function, respectively. In current paper, we utilized the minimum prediction risk principle with using final prediction error (FPE) [20] to find the best and optimum topology of our proposed WNN. The prediction risk $P_\lambda$ measures the generalization ability of network and is defined as below for network:

$$ P_\lambda = \int \left[ dx \ p(x) \left[ \mu(x) - \hat{\mu}(x) \right]^2 + \kappa \right] = E \left[ \frac{1}{n} \sum_{p=1}^{n} (y_p - \hat{y}_p)^2 \right] $$

(20)

where, $\mu(x)$ is an unknown function, $p(x)$ is stationary probability density function, $\kappa$ is the variance of independent random variables. Also, $(x^*_p, y^*_p)$ are the new observations that were not used in the construction of the network and $\hat{y}_p$ is the network output for $x^*_p$. Since finding the prediction risk is not a straight forward procedure, we used (FPE) criterion as reported in literature [20]:

$$ P_\lambda = \frac{1 + k}{2n - 2k} \sum_{p=1}^{n} (y_p - \hat{y}_p)^2 $$

(21)

where, $k$ is the number of parameters of the network and $n$ is the number of training patterns in the training sample. The target value is given by $y_p$, and $\hat{y}_p$ the approximation of the target value by the network. To find the optimum topology of WNN the algorithm is followed as below. At first a WNN without any hidden unit is constructed. So, the network is trained and then the prediction risk is estimated by FPE. Next, 1 hidden unit is added to hidden layer and the network training and prediction risk estimation is repeated. We continued the procedure by adding hidden unit and repeating network training and prediction risk estimation until we reach to the predefined maximum number of hidden units. The number of hidden units relevant to smallest prediction risk define the optimum number of wavelets for the best topology of network.

The algorithm is illustrated in Figure 3. Also, Figure 4 shows the prediction risk versus number of hidden units for our proposed WNN. As it is clear, the optimum number occurred in 73 units with 1.379 prediction risk.

5. WNN SOLUTION FOR FKP

In order to solve the FKP of 6-RSU mechanism by means of WNN, the rotation angles of revolute joints in joint-space, $X = (\theta_1, \theta_2, ..., \theta_6)$ are considered as input data and Along with the training samples are feed to the network for process training procedure. To approximate the kinematics model of the 6-RSU mechanism, the algorithm of wavelet neural network is summarized in 5 steps.

Step 1: Set the initial values of the momentum factor $\sigma$, rate of learning $\lambda$ and the parameters of network $(W^{(1)}, W^{(2)}, \Theta^{(1)}, \Theta^{(2)}, a_1, a_2, b_1, ..., b_p)$.  

Step 2: Give the input vectors $X = (\theta_1, \theta_2, ..., \theta_6)$ and desired output vector $\mathbf{Y}_q = (\bar{x}_q, \bar{y}_q, \bar{z}_q, \bar{\alpha}_q, \bar{\beta}_q, \bar{\gamma}_q)$ as the training data to handle the training of network. The exact theoretical values of training data were obtained by inverse kinematic solution from Equation (8). 

Step 3: Estimate the output of the WNN by Equation (16) for each input data.

Step 4: Regulate the networks parameters employing gradient descent algorithm by Equation (19).

Step 5: The total error of the proposed network is estimated by Equation (18).
If the error is in the desired range, the networks parameters are determined and the learning process is completed, else restart the learning procedure.

6. SUMULATION AND RESULTS

The results of the proposed WNN on approximating the forward kinematic analysis of the 6-RSU mechanism are presented in this section. The proposed structure for designed wavelet network has one input layer with six neurons, one hidden layer with 73 neurons and one output layer with six neurons. The network was trained with a learning rate of 0.21, a momentum term of 0.55, and 1024 learning iterations. The largest error E or given precision is less than 0.6%. First, using inverse kinematic solution for the Hexarot, the closed form solution (CFS) were obtained for two different paths (paths I and II). Data extracted by path (I) is feed to train the network. Besides, to verify the performance of network after training, path (II) is applied. Figures 5 to 10 show the results of the proposed WNN using the path (I) for simulation.

Using the inverse kinematic analysis for proposed paths, the motions of the each upper arm is defined. Then, the proposed WNN is feed by the arms motions to get the trajectory and movement paths of the manipulated platform. Again, the outputs of the proposed WNN are employed for inverse kinematic analysis to define the new motions of the arms and to the comparison with those obtained by CFS.

Figures 5 to 7 show the results for joint-space and angular position for all six arms During Path (I). Figures 8 and 9 indicate the results for position and orientation of manipulated platform, respectively. Also, the results displayed in Figure 10 show the position of manipulated platforms in 3D view. These results are employed to train the WNN. However, verification of the proposed WNN is executed by path (II). The results are illustrated in Figures 11 to 16. Figures 11 to 13 present the comparison of the results between WNN and CFS for the movements of the arms in joint space during path (II).

Figures 14, 15 and 16 illustrate the CFS and WNN results in work-space included position, orientation and spatial displacement for the manipulated platform.

According to the results illustrated in Figures 5 to 16 there is good agreement between the exact solution (CFS) and the outputs of proposed WNN. The errors are less than %1 and it demonstrates the efficiency and superiority of the WNN as a powerful method to approximate the highly nonlinear dynamic systems.
Figure 8. Results for Work-Space kinematic parameters During Path (I) – Position of Manipulated Platform

Figure 9. Results for Work-Space kinematic parameters During Path (I) – Orientation of Manipulated Platform

Figure 10. 3D Plot for Position Results of Manipulated Platform During Path (I) by CFS and WNN

Figure 11. Results for Joint-Space kinematic parameters During Path (II) – Angular Position for Arms 1 and 2

Figure 12. Results for Joint-Space kinematic parameters During Path (II) – Angular Position for Arms 3 and 4

Figure 13. Results for Joint-Space kinematic parameters During Path (II) – Angular Position for Arms 5 and 6
To estimate the training and computing time for proposed WNN, the “tic” and “toc” functions were used in the code written in MATLAB. The training time for 1024 learning iteration is 20.68 (s) and the computing time for simulation after training the network is less than 0.2 (s). So, the proposed WNN can be employed to practical applications.

7. CONCLUSIONS

The main goal of the current contribution is the application of wavelet neural network as a useful tool to solve the forward kinematics problem of the Hexarot. To this end, using the vectorial and geometrical principles, the kinematic model of the mechanism is obtained and the inverse kinematic problem is solved. Due to the difficulty of the forward kinematic analysis of the parallel mechanisms and the serious impediments of the classical numerical algorithms, neural network analysis based on wavelet functions is proposed. Therefore, the inverse kinematic analysis is employed to provide data for network training and verification. Back propagation algorithm and the iterative gradient descent method are used to minimize the total error of the network and to formulate the WNN parameters. The minimum prediction risk principle with using final prediction error are utilized to find the best and optimum topology of our proposed WNN. The proposed WNN are exerted to the different paths and the accurate results are generated. According to training approach of the network the maximum error is less than 0.6%. So, the comparison of the results obtained by WNN with the CFS indicates the accurate performance and the superiority of the proposed neural network algorithm.

8. REFERENCES

Application of Wavelet Neural Network in Forward Kinematics Solution of 6-RSU Co-axial Parallel Mechanism Based on Final Prediction Error

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Keywords:
Wavelet Neural Network
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Final Prediction Error

Abstract

In this study, a novel co-axial parallel mechanism (RSU) is proposed for solving the forward kinematics problem. The kinematic characteristics of this mechanism are complex due to the presence of both rotational and linear active links. A wavelet neural network (WNN) with random wavelet hidden layers is used to approximate the forward kinematics of the RSU mechanism. The proposed WNN is trained using the final prediction error (FPE) method, which is a type of supervised learning. The performance of the WNN is evaluated by comparing the output of the network with the analytical solution of the forward kinematics problem.

Keywords:
Forward kinematics
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